

Best constant in Hyers-Ulam stability of some functional equations

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ABSTRACT.

We obtain the infimum of Hyers-Ulam constants for Cauchy, Jensen and Quadratic functional equations. Moreover, in each case the infimum is itself a Hyers-Ulam constant.

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