

On some convergences to the constant e and improvements of Carleman's inequality

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ABSTRACT.

We present sharp inequalities related to the sequence $(1 + 1/n)^n$ and some applications to Kellers' limit and Carleman's inequality.

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