

Collectively coincidence results for lower semicontinuous multifunctions in locally convex spaces

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ABSTRACT. In this paper we present coincidence results between lower semicontinuous type maps and *HLPY* type maps. Our arguments are based on the Schauder-Tychonoff fixed point theorem and Michael's selection theorem.

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