

# A Voronovskaya type theorem associated to geometric series of Bernstein - Durrmeyer operators

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**ABSTRACT.** In this paper we give a Voronovskaya type theorem for the operators introduced by U. Abel, which are defined as the geometric series of Bernstein - Durrmeyer operators.

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