

Semi-exponential Post-Widder operators

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ABSTRACT. This paper focuses on the Post-Widder operators of semi-exponential type. We present an alternative and straightforward approach using Laplace transforms to analyze these operators. Additionally, we derive specific results concerning various moduli of continuity.

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